

# Natural Experiments and Difference-in-Differences

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# Objectives

- Provide a basic introduction to natural experiments and difference-in-differences methods in observational studies
  - Provide examples of these methods
  - Not meant for those already experienced with these methods
  - No advanced topics covered
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# Outline

- Causality and study design
  - Natural Experiments
  - Difference-in-differences
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# Poll 1

*Select one option*

- I'm experienced in diff-in-diff
  - I know a little about diff-in-diff
  - What's diff-in-diff?
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# Outline

- Causality and study design
  - Natural Experiments
  - Difference-in-differences
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# Causality

- In HSR, we often study impact of implementing new program, intervention, or policy.
  - Ideally, would estimate causal effect of treatment on outcomes by comparing outcomes under counterfactual
    - Treatment effect= $Y_i(1)-Y_i(0)$
    - Observe outcome  $Y$  when patient gets treatment,  $t=1$  and when same patient does not get treatment,  $t=0$
    - Compare difference in outcomes to get impact of treatment
    - In reality we don't observe same patients with and without treatment
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# Randomized Study Design

- Randomize who gets treatment T

R      T      O

R                      O

- Compare outcome between treated and untreated groups to get impact of treatment
  - Because treatment was randomized, there are no systematic differences between treated and untreated groups.
  - Differences in outcomes can be attributed to causal effect of treatment
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# Estimating Treatment Effect

- Randomize Program P: 0=no, 1=yes

$$Y = \beta_0 + \beta_1 P + \varepsilon$$

- $\beta_1$  is average treatment effect
  - Assumption that error term ( $\varepsilon$ ) is uncorrelated with program (P) assignment
    - Error term ( $\varepsilon$ ) is exogenous
    - $\beta_1$  is unbiased
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# Causality and Observational Studies

- Randomization, e.g. randomized controlled trials (RCT), not commonly used for programs, policies, and many treatments
  - Most HSR is observational
    - Causality difficult to show because of confounding (endogeneity)
    - Error term ( $\varepsilon$ ) correlated with program (P) assignment and endogenous
    - Estimate of treatment effect ( $\beta_1$ ) is biased
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# Poll 2

*Select one option*

- Randomization removes systematic differences b/t trt and control groups
  - Correlation b/t error term and trt leads to unbiased estimates of trt effect
  - Multivariable analysis eliminates all bias from endogeneity
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# Outline

- Causality and study design
  - Natural Experiments
  - Difference-in-differences
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# Natural Experiments

- Type of quasi-experimental design
  - Assignment of program/treatment (often unintended) is due to exogenous variation
    - Variation across time and events
  - Mimics features of a randomized study
  - Need to consider context
  - Generalizability can be limited
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# Examples of Natural Experiments

- Lottery prize winners and health outcomes (Lindahl, 2005)
  - Voluntary state Medicaid expansion to higher-income individuals under ACA (Sommers, 2015)
  - CA first state to pass law on minimum nurse staffing ratios in acute care hospitals in 1999 (Mark, 2009)
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# Comparing Outcomes in Natural Experiments

- One approach involves ignoring control group and use change in mean outcome in treatment group over time (pre-treatment/post-treatment)
  - $Y = \beta_0 + \beta_1 \text{Post} + \varepsilon$
  - $\text{Post}=0$ , pre-treatment period
  - $\text{Post}=1$ , post-treatment period
  - $\beta_1$  biased if change unrelated to program/policy
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# Comparing Outcomes in Natural Experiments

- Another approach is compare mean outcome between treatment and control groups only in the post-treatment period
  - $Y = \beta_0 + \beta_1 \text{Treatment} + \varepsilon$
  - Treatment=0, control group
  - Treatment=1, treatment group
  - $\beta_1$  biased if there are unmeasured differences between groups
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# Outline

- Causality and study design
  - Natural Experiments
  - Difference-in-differences
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# Difference-in-Differences

- Often applied to natural experiments
  - Need data for at least two time periods for two groups-- treatment and control group
  - Subtract out differences between treatment and control groups and differences over time
  - Assumes similar time trend between groups
  - If treatment as if randomly received, then causal effect can be estimated through OLS
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# Diff-in-Diff Regression

$$Y = \beta_0 + \beta_1 \text{Post} + \beta_2 \text{Treatment} + \beta_3 \text{Post} * \text{Treatment} + \varepsilon$$

- Mean outcome for control group in pre-period

$$\bar{Y} = \beta_0$$

- Mean outcome for control group in post-period

$$\bar{Y} = \beta_0 + \beta_1$$

- Mean outcome for treatment group in pre-period

$$\bar{Y} = \beta_0 + \beta_2$$

- Mean outcome for treatment group in post-period

$$\bar{Y} = \beta_0 + \beta_1 + \beta_2 + \beta_3$$

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# Diff-in-Diff Estimator

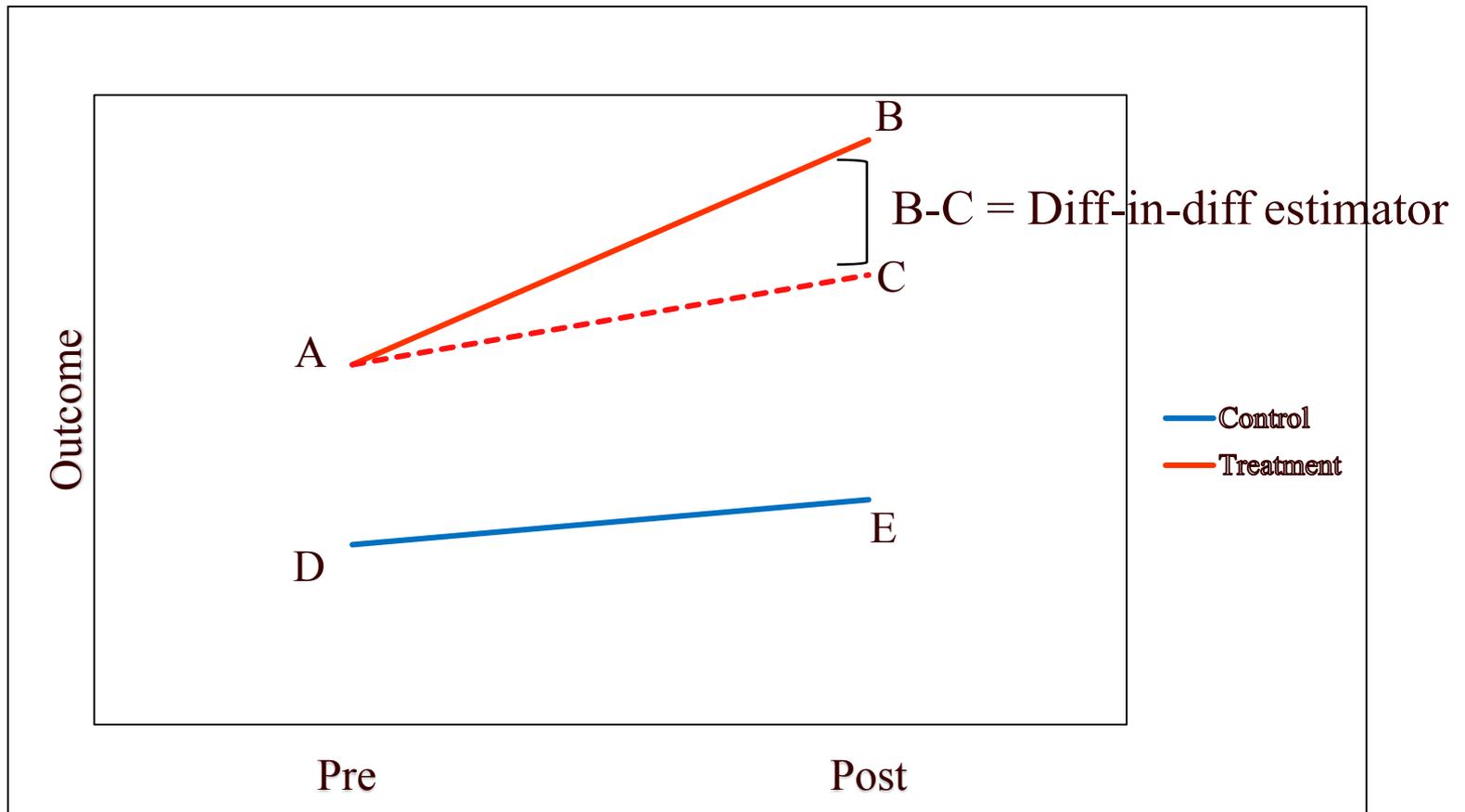
$$Y = \beta_0 + \beta_1 \text{Post} + \beta_2 \text{Treatment} + \beta_3 \text{Post} * \text{Treatment} + \varepsilon$$

$$(\bar{Y}^{\text{Treatment, Post}} - \bar{Y}^{\text{Treatment, Pre}}) - (\bar{Y}^{\text{Control, Post}} - \bar{Y}^{\text{Control, Pre}})$$

$$[(\beta_0 + \beta_1 + \beta_2 + \beta_3) - (\beta_0 + \beta_2)] - [(\beta_0 + \beta_1) - \beta_0] = \beta_3$$

- $\beta_3$  is the difference-in-differences estimator
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# Chart for Diff-in-Diff



# Strengths and Weaknesses

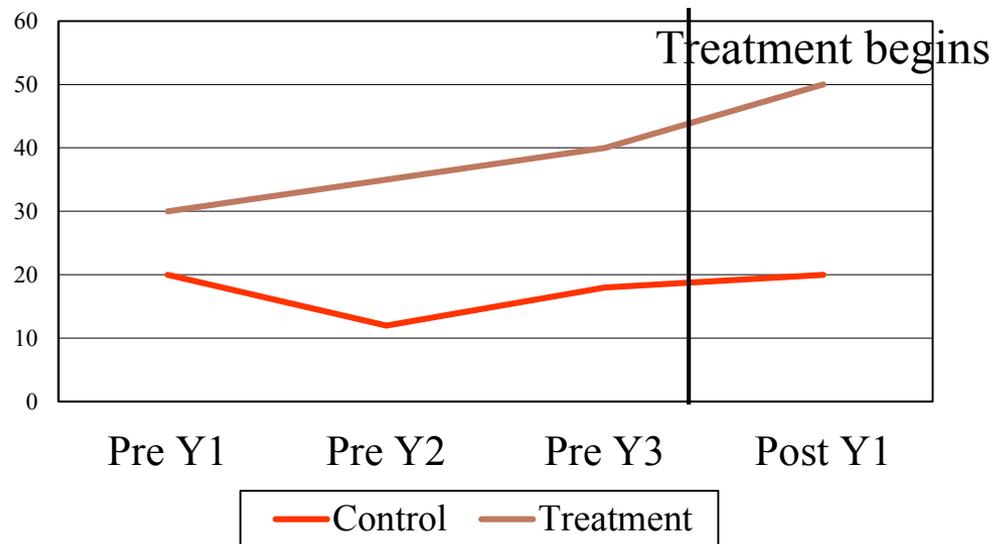
- Strengths
    - Eliminates any pre-treatment differences in outcome between groups
    - Difference out time trend in treatment group
  - Weaknesses
    - If unobserved factors that change over time, can have biased estimates
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# Panel data and Diff-Diff

- $Y_{it} = \beta_0 + \beta_1 T_{it} + \beta_2 \text{Post}_{it} + \gamma_i + \varepsilon_{it}$
  - $Y_{i2} - Y_{i1} = \beta_1(T_{i2} - T_{i1}) + \beta_2 + \beta_3(T_{i2} - T_{i1}) + (\varepsilon_{i2} - \varepsilon_{i1})$
  - $\Delta Y_i = \beta_1 \Delta T_i + \beta_2 + \Delta \varepsilon_i$
  - Addresses omitted variables bias if unmeasured time invariant factors
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# Test of Natural Experiments and Diff-in-Diff

- Parallel trends assumption
- Examine trends in pre-treatment period



# Test of Natural Experiments and Diff-in-Diff

- Measure outcomes not likely to be affected by treatment
  - Significant differences only for outcomes expected to be impacted by treatment
    - Suggests causal association between treatment and outcomes of interest
  - Significant differences both for outcomes expected to be impacted by treatment and unrelated outcomes
    - Suggests not causal association for treatment and outcomes of interest
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# Threats to Validity

## Internal Validity

- Imperfect randomization  $\longrightarrow$  Instrumental Variables
- Failure to follow treatment protocol/attrition
- Treatment variation is not exogenous

## External validity

- Non-representative treatment or sample
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# D-D Example

- Sommers, Benjamin D., et al. "Changes in self-reported insurance coverage, access to care, and health under the Affordable Care Act." *Jama* 314.4 (2015): 366-374.
  - Voluntary Medicaid expansion to higher income adults by state in 2014
  - 28 states had Medicaid expansion and 22 did not by March 2015
  - Measure outcomes from 2012 and 2015 in low-income adults
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# D-D Example

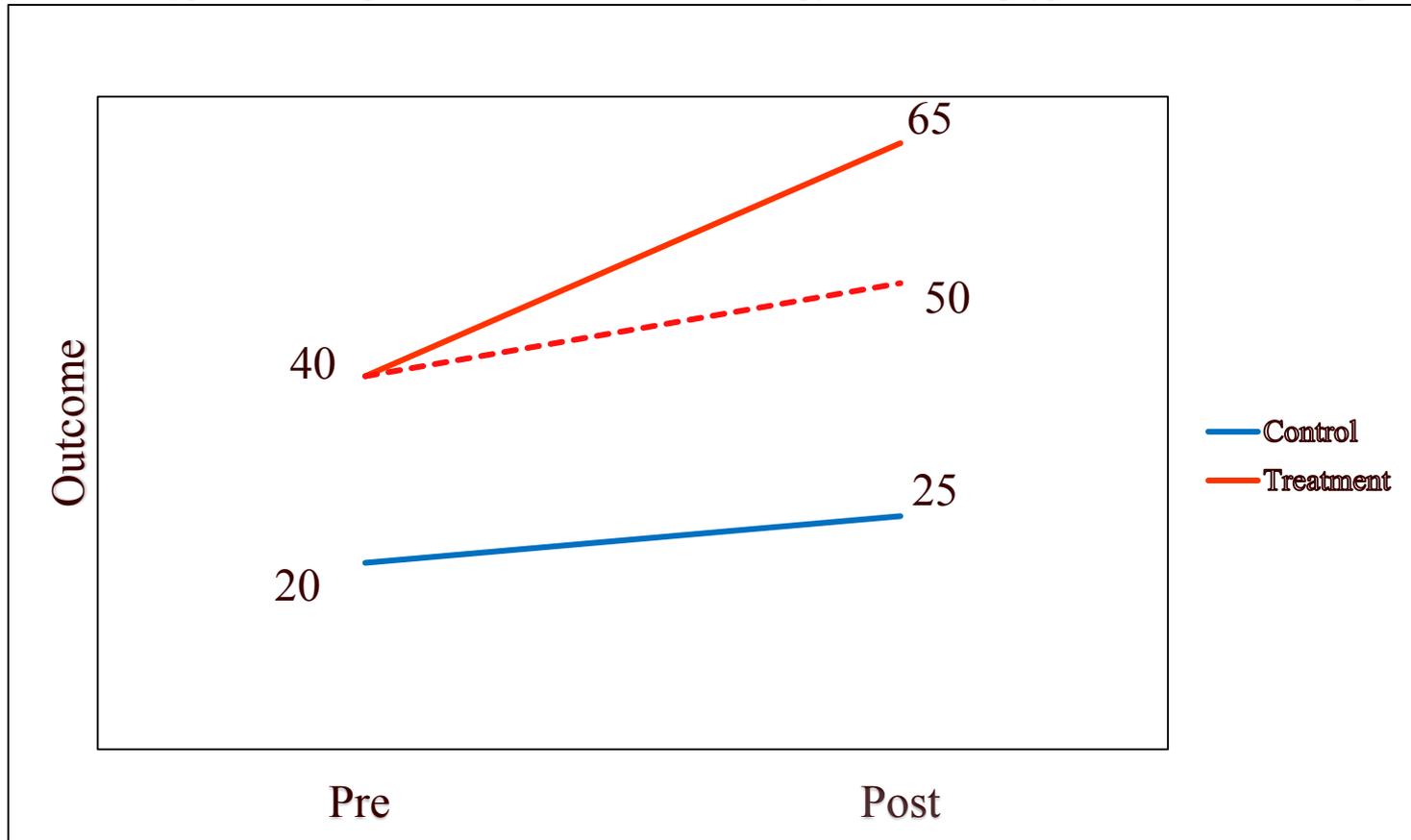
Table 4. Changes in Self-reported Coverage, Access to Care, and Health Among Low-Income Adults in Medicaid Expansion vs Nonexpansion States

Outcome	States, Unadjusted Mean, % (95% CI) <sup>a</sup>				Differences-in-Differences Adjusted Estimate	
	Medicaid Expansion (n = 48 905)		Nonexpansion (n = 37 283)		Net Change After ACA (95% CI)	P Value
	Before ACA <sup>b</sup>	After ACA <sup>c</sup>	Before ACA <sup>b</sup>	After ACA <sup>c</sup>		
Uninsured	35.9 (35.3 to 36.5)	26.5 (25.8 to 27.3)	44.3 (43.5 to 45.0)	39.7 (38.9 to 40.6)	-5.2 (-7.9 to -2.6)	<.001
No personal physician	38.5 (37.8 to 39.1)	35.8 (35.0 to 36.7)	43.0 (42.3 to 43.7)	43.0 (42.0 to 44.0)	-1.8 (-3.4 to -0.3)	.02
No easy access to medicine	17.3 (16.8 to 17.8)	15.0 (14.4 to 15.7)	18.8 (18.2 to 19.4)	18.7 (17.9 to 19.5)	-2.2 (-3.8 to -0.7)	.005
Cannot afford care	35.5 (34.9 to 36.1)	33.1 (32.3 to 33.9)	40.2 (39.5 to 41.0)	39.5 (38.5 to 40.5)	-1.3 (-3.7 to 1.0)	.27
Fair/poor health	34.2 (33.6 to 34.8)	34.9 (34.0 to 35.7)	34.3 (33.6 to 35.0)	34.1 (33.2 to 35.1)	-0.1 (-1.7 to 1.4)	.84
% of Last 30 d in which activities were limited by poor health	16.4 (16.0 to 16.8)	16.6 (16.0 to 17.1)	17.4 (17.0 to 17.9)	17.2 (16.6 to 17.8)	-0.1 (-0.9 to 0.7)	.78

Sommers, Benjamin D., et al. "Changes in self-reported insurance coverage, access to care, and health under the Affordable Care Act." *Jama* 314.4 (2015): 366-374.

# Poll 3

## What is the Diff-in-diff estimator?



Possible responses: A. 10    B. 15    C. 25

# Review

- Quasi-experimental methods can help address common sources of bias of treatment effects in observational studies.
  - Natural experiments are a type of quasi-experimental design that exploit variation in implementation of treatments/ programs/ policies
  - Difference-in-differences is frequently used in natural experiments since it can difference out any pre-treatment and post-treatment changes in outcomes not related to the treatment itself
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# References

- Stock, James H., and Mark W. Watson. *Introduction to econometrics*. 2015.
  - Wooldridge, J. M.: *Econometric Analysis of Cross Section and Panel Data*. MIT Press, Cambridge, Mass., 2002.
  - Campbell, D. T., and Stanley, J. C. *Experimental and Quasi-experimental Designs for Research*. Chicago: Rand McNally, 1966.
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# More References

Sommers, Benjamin D., et al. "Changes in self-reported insurance coverage, access to care, and health under the Affordable Care Act." *Jama* 314.4 (2015): 366-374.

Lindahl, Mikael. "Estimating the effect of income on health and mortality using lottery prizes as an exogenous source of variation in income." *Journal of Human resources* 40.1 (2005): 144-168.

Mark, Barbara, David W. Harless, and Joanne Spetz. "California's minimum-nurse-staffing legislation and nurses' wages." *Health Affairs* 28.2 (2009): w326-w334.

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# Next Lectures

*Feb 20, 2019*

**Regression Discontinuity**

Liam Rose, Ph.D.

*Feb 27, 2019*

**Instrumental Variables**

Wei Yu, Ph.D.

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# Questions?

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